

Electron-Phonon Coupling in Naphthalene

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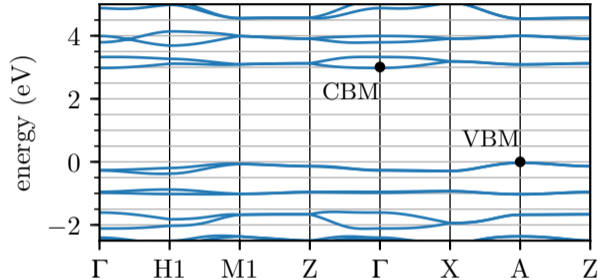
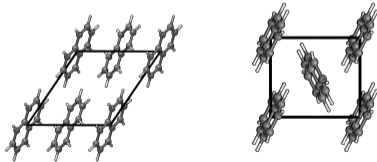
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Outline

- 1** Introduction
- 2** Recent implementation in Abinit
- 3** Temperature dependence of the band gap
- 4** Electron and hole mobilities
- 5** Self-consistency in the self-energy

Naphthalene crystals

- Organic molecular crystal
- Good electrical conductivity
 - ▶ Solar cell
 - ▶ Field-effect transistors



- Zero-point renormalization (ZPR)
- Temperature-dependent band gap
- Electron and hole mobilities

Computing the electron-phonon self-energy

Fan self-energy

$$\Sigma_{\mathbf{k}n}^{\text{Fan}}(T, \omega) = \sum_{\mathbf{q}\nu} \sum_m |g_{m\nu}(\mathbf{k}, \mathbf{q})|^2 \left[\frac{n_{\mathbf{q}\nu}(T) + f_{\mathbf{k}+\mathbf{q}m}(T)}{\varepsilon - \varepsilon_{\mathbf{k}+\mathbf{q}m} + \hbar\omega_{\mathbf{q}\nu} + i\eta} + \frac{n_{\mathbf{q}\nu}(T) + 1 - f_{\mathbf{k}+\mathbf{q}m}(T)}{\varepsilon - \varepsilon_{\mathbf{k}+\mathbf{q}m} - \hbar\omega_{\mathbf{q}\nu} + i\eta} \right]$$

Separation into lower bands / higher bands contributions

$$\Sigma(T, \omega) = \sum_{\mathbf{q}\nu} \sum_{m \leq M} \Sigma_{\mathbf{q}\nu, m}(T, \omega) + \sum_{\mathbf{q}\nu} \sum_{m > M} \Sigma_{\mathbf{q}\nu, m}^{\text{Static}}(T, \varepsilon_{\mathbf{k}n}^0)$$

Double-grid technique

$$\Sigma(T, \omega) = \sum_{\mathbf{q}\nu}^{\text{fine}} \sum_{m \leq M} \Sigma_{\mathbf{q}\nu, m}(T, \omega) + \sum_{\mathbf{q}\nu}^{\text{coarse}} \sum_{m > M} \Sigma_{\mathbf{q}\nu, m}(T, \varepsilon_{\mathbf{k}n}^0)$$

Interpolating the phonon potential in polar materials

Long-range part of the phonon potential

$$V_{\kappa j}^L(\mathbf{q}, \mathbf{r}) = i \frac{4\pi}{\Omega} \sum_{\mathbf{G}} \frac{e^{i(\mathbf{q}+\mathbf{G})\cdot(\mathbf{r}-\mathbf{R}_{\kappa})} (\mathbf{q} + \mathbf{G})_{j'} \cdot Z_{\kappa, j' j}^*}{(\mathbf{q} + \mathbf{G}) \cdot \boldsymbol{\varepsilon}^{\infty} \cdot (\mathbf{q} + \mathbf{G})}$$

Fourier interpolation of the short-range part of the phonon potential

$$W_{\kappa j}^S(\mathbf{r} - \mathbf{R}_l) = \sum_{\mathbf{q}} e^{i\mathbf{q}\cdot\mathbf{R}_l} \left[V_{\kappa j}(\mathbf{q}, \mathbf{r}) - V_{\kappa j}^L(\mathbf{q}, \mathbf{r}) \right]$$

The long-range part is then added to the interpolated potential

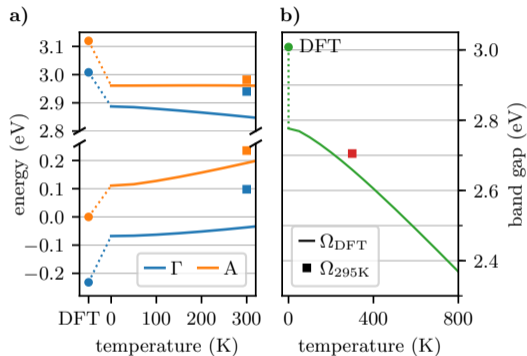
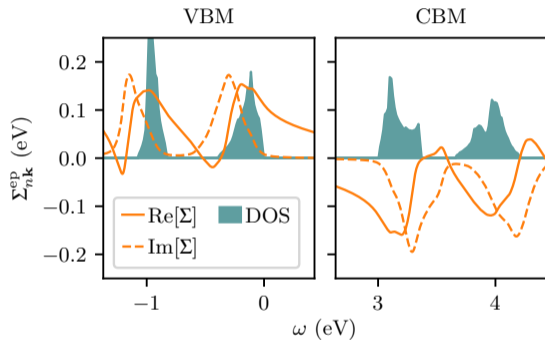
$$V_{\kappa j}(\tilde{\mathbf{q}}, \mathbf{r}) \approx \sum_l W_{\kappa j}^S(\mathbf{r} - \mathbf{R}_l) e^{-i\tilde{\mathbf{q}}\cdot\mathbf{R}_l} + V_{\kappa j}^L(\tilde{\mathbf{q}}, \mathbf{r})$$

Workflow

Computation	Executable	Input variables	Files
Eigenvalues at \mathbf{k} and at $\mathbf{k} + \mathbf{q}$	abinit	iscf=-2	EIG.nc
DFPT calculation of all perturbations (atoms + electric field)	abinit	rfphon=1	POTx DDB.nc
Non-self-consistent DFPT for upper bands contribution	abinit	rfphon=1 ieig2rf=5 iscf=-2	EIGR2D.nc
Merging of phonon potential	mrgdv		DVDB
Interpolation of phonon potential	abinit	eph_task=5	DVDB
Merging of dynamical matrices	mrgddb		DDB
Interpolation of dynamical matrices	anaddb	prtddb=1	DDB.nc
El-ph coupling matrix elements	abinit	eph_task=2	GKK.nc
Self-energy	ElectronPhonon-Coupling		EP.nc

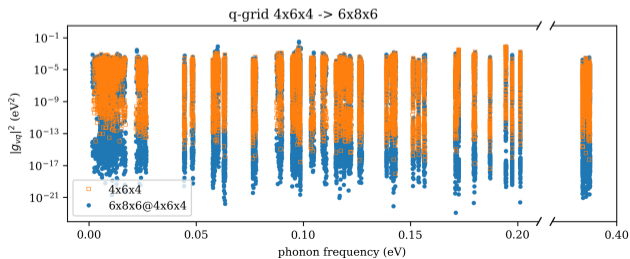
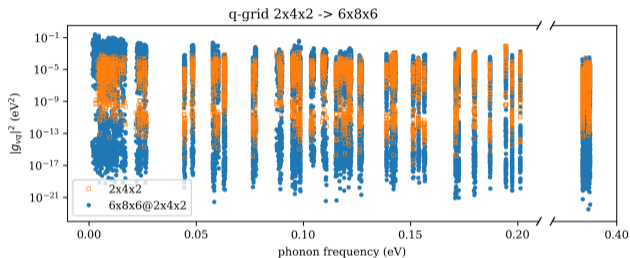
Temperature dependence of the band gap

Band gap renormalization



	Exp.	DFT	GW	GW+ZPR
Band gap (eV)	5.0	3.01	5.30	5.07

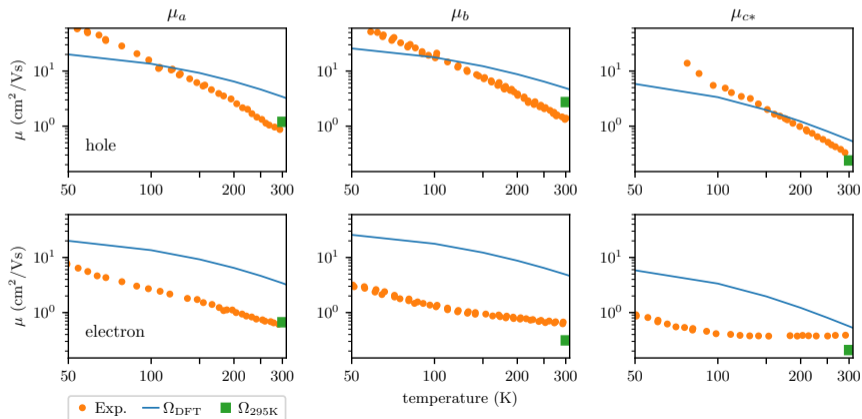
A word of warning



- Large errors in the interpolated potential with a $2 \times 4 \times 2$ coarse q-point grid

Electrical mobility

$$\mu_{\alpha}^{e,h} = \frac{-e}{\rho_{e,h}\Omega} \sum_n \int \frac{d\mathbf{k}}{\Omega_{\text{BZ}}} \frac{\partial f_{n\mathbf{k}}}{\partial \varepsilon_{n\mathbf{k}}} |v_{n\mathbf{k},\alpha}|^2 \tau_{n\mathbf{k}}$$



Approximating the mobility

Using the density of states $D(\varepsilon)$

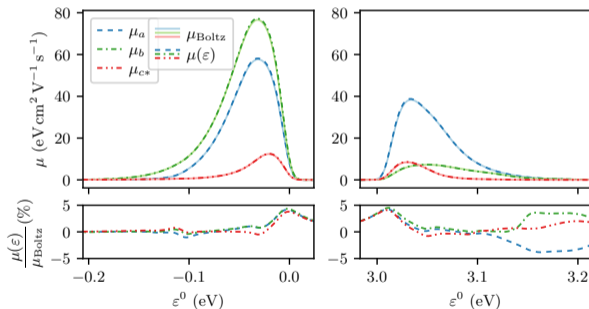
$$\mu_{\alpha}^{\text{e,h}} \approx \frac{-e}{\rho_{\text{e,h}}} \int d\varepsilon D(\varepsilon) f'(\varepsilon) v_{\alpha}^2(\varepsilon) \tau(\varepsilon)$$

Energy-resolved squared velocity

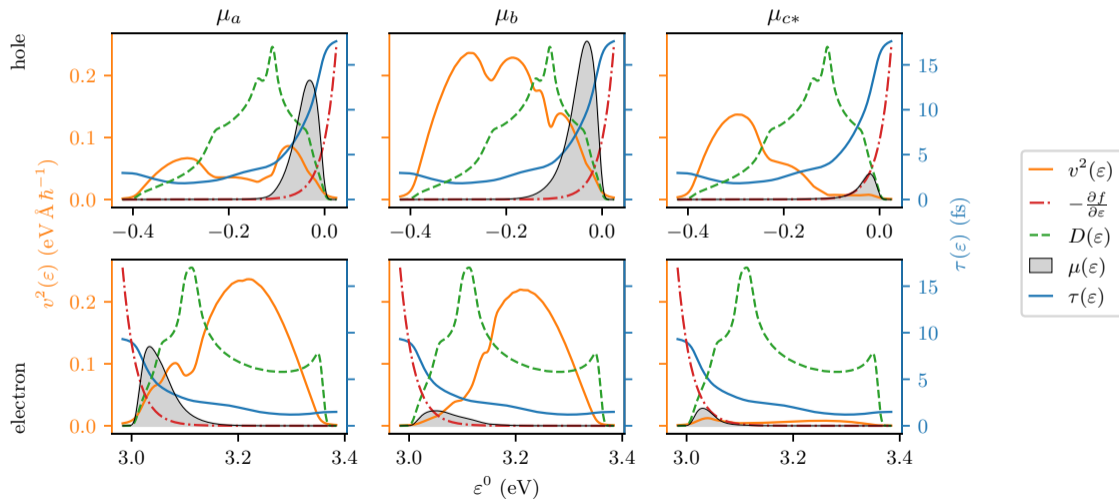
$$v_{\alpha}^2(\varepsilon) = \frac{1}{D(\varepsilon)} \sum_n \int \frac{d\mathbf{k}}{\Omega_{\text{BZ}}} |v_{n\mathbf{k},\alpha}|^2 \delta(\varepsilon - \varepsilon_{n\mathbf{k}})$$

Energy-resolved lifetime

$$\tau(\varepsilon) = \frac{1}{D(\varepsilon)} \sum_n \int \frac{d\mathbf{k}}{\Omega_{\text{BZ}}} \tau_{n\mathbf{k}} \delta(\varepsilon - \varepsilon_{n\mathbf{k}})$$



Approximating the mobility



Self-consistency in the self-energy

Finding the quasiparticle energy

On-the-mass-shell approximation

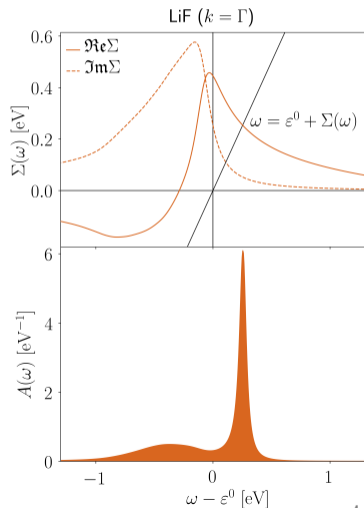
$$\varepsilon_{\mathbf{k}n}(T) = \varepsilon_{\mathbf{k}n}^0 + \Re\Sigma_{\mathbf{k}n}(\varepsilon_{\mathbf{k}n}^0, T)$$

Quasiparticle energy

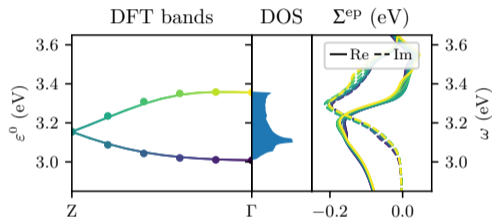
$$\varepsilon_{\mathbf{k}n}(T) = \varepsilon_{\mathbf{k}n}^0 + \Re\Sigma_{\mathbf{k}n}(\varepsilon_{\mathbf{k}n}, T)$$

Spectral function

$$\begin{aligned} A_{\mathbf{k}n}(\omega, T) &= \frac{1}{\pi} \Im G_{\mathbf{k}n}(\omega, T) \\ &= \frac{1}{\pi} \frac{|\Im\Sigma_{\mathbf{k}n}(\omega, T)|}{[\omega - \varepsilon^0 - \Re\Sigma_{\mathbf{k}n}(\omega, T)]^2 + \Im\Sigma_{\mathbf{k}n}(\omega, T)^2} \end{aligned}$$



Self-consistent scheme



The self-energy is largely k-independent

Iterative computation of the self-energy at Γ

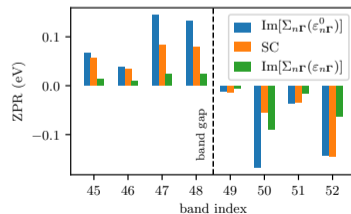
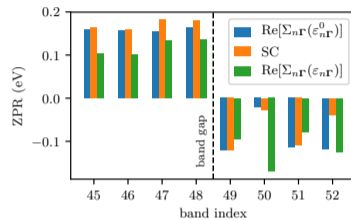
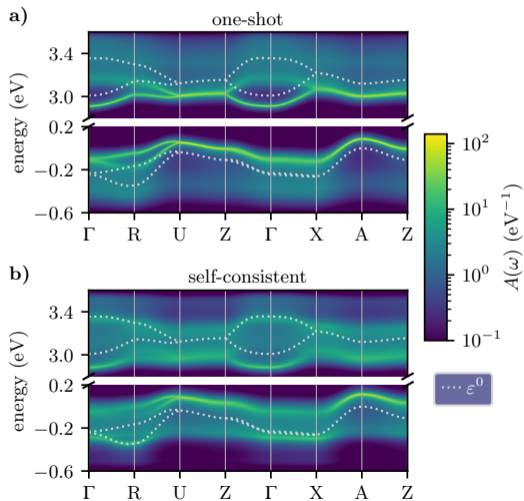
$$\epsilon_{nk}^1 = \epsilon_{nk}^0 + \Re[\Sigma_{n\Gamma}(\{\epsilon_{nk}^0 - \epsilon_{mk+\mathbf{q}}^0 \pm \omega_{\mathbf{v}\mathbf{q}}\})]$$

$$\epsilon_{nk}^2 = \epsilon_{nk}^0 + \Re[\Sigma_{n\Gamma}(\{\epsilon_{nk}^1 - \epsilon_{mk+\mathbf{q}}^1 \pm \omega_{\mathbf{v}\mathbf{q}}\})]$$

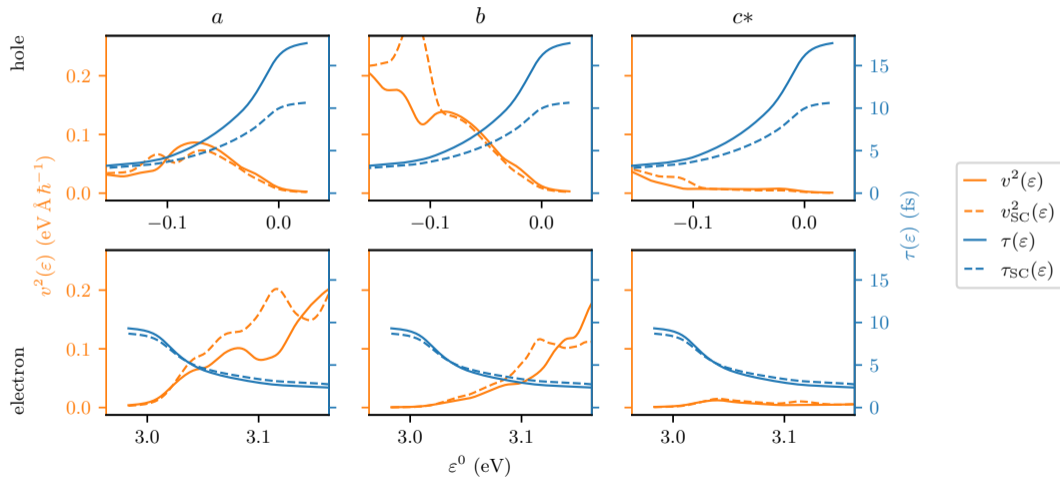
...

$$\epsilon_{nk}^i = \epsilon_{nk}^0 + \Re[\Sigma_{n\Gamma}(\{\epsilon_{nk}^{i-1} - \epsilon_{mk+\mathbf{q}}^{i-1} \pm \omega_{\mathbf{v}\mathbf{q}}\})],$$

Self-consistent scheme



Effect of self-consistency on the mobility



Effect of self-consistency on the mobility

	Mobility at 295K					
	μ_a^h	hole μ_b^h	μ_{c*}^h	electron μ_a^e	μ_b^e	μ_{c*}^e
one-shot	1.20	2.73	0.24	0.67	0.31	0.21
SC	0.90	2.19	0.18	1.18	0.59	0.31
Exp.	0.79	1.34	0.31	0.58	0.63	0.39

Summary / Acknowledgments

- Efficient scheme for computing the electron-phonon self-energy
- Interpolation of the phonon coupling potential in real space
- Good agreement for the band gap and ZPR of Naphthalene
- Reasonable agreement for the electron and hole mobilities
- Important effect of lattice expansion on mobilities
- Self-consistent electron-phonon self-energy scheme
- On-the-mass-shell approximation better mimics self-consistency

Thank you for your attention!

